

Solve the differential equation.

1)  $\frac{dy}{dx} = \frac{y}{x}$

2)  $y' = y^2 \sin x$

3)  $(1 + \tan y)y' = x^2 + 1$

$$4) \frac{du}{dt} = 2 + 2u + t + tu$$

$$5) \frac{dz}{dt} + e^{t+z} = 0$$

Find the solution of the differential equation that satisfies the given initial condition.

$$6) \frac{dy}{dx} = y^2 + 1, \quad y(1) = 0$$

7)  $\frac{dy}{dx} = \frac{y \cos x}{1 + y^2}, \quad y(0) = 1$

8)  $\frac{dP}{dt} = \sqrt{Pt}, \quad P(1) = 2$

9) Find an equation of the curve that satisfies  $\frac{dy}{dx} = 4x^3 y$  and whose  $y$ -intercept is 7.

10) Find an equation of the curve that passes through the point  $(1, 1)$  and whose slope at  $(x, y)$  is  $\frac{y^2}{x^3}$ .

11) A tank contains 1000 L of brine with 15 kg of dissolved salt. Pure water enters the tank at a rate of 10 L/min. The solution is kept thoroughly mixed and drains from the tank at the same rate. How much salt is in the tank after  $t$  minutes and after 20 minutes?